

**Section A: Multiple Choice / Afdeling A: Meervoudige keuse****Time: 45 minutes Marks: 20 / Tyd: 45 minute Punte: 20**

The questions in Section A must be completed on SIDE 2 of the optical reader form in SOFT PENCIL.

Die vrae in Afdeling A moet op KANT 2 van die merkleesvorm in SAGTE POTLOOD voltooi word.

**Question 1 / Vraag 1**

For the piece-wise defined function / Vir die stuksgewys-gedefinieerde funksie

$$f(x) = \begin{cases} 2 & \text{if } |x| \leq 1 \\ 3 - x & \text{if } |x| > 1 \end{cases}$$

Which statement is true? / Watter bewering is waar?

1a.	The domain of $f$ is $[0, \infty)$ and the range is $\mathbb{R}$ .
1b.	The domain of $f$ is $\mathbb{R}$ and the range is $(-\infty, 2] \cup [4, \infty)$ .
1c.	The domain of $f$ is $\mathbb{R}$ and the range is $\mathbb{R} \setminus (2, 4)$ .
1d.	The domain of $f$ is $[0, \infty)$ and the range is $(-\infty, 2]$ .
1e.	None of the above

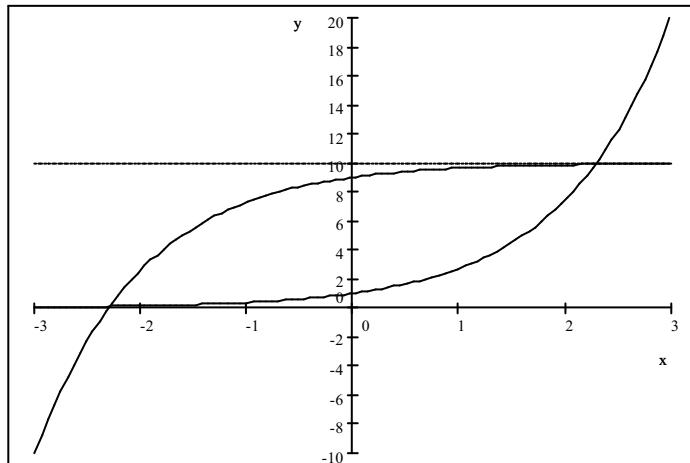
1a.	Die definisieversameling van $f$ is $[0, \infty)$ en die waardeversameling van $f$ is $\mathbb{R}$ .
1b.	Die definisieversameling van $f$ is $\mathbb{R}$ en die waardeversameling van $f$ is $(-\infty, 2] \cup [4, \infty)$ .
1c.	Die definisieversameling van $f$ is $\mathbb{R}$ en die waardeversameling van $f$ is $\mathbb{R} \setminus (2, 4)$ .
1d.	Die definisieversameling van $f$ is $[0, \infty)$ en die waardeversameling van $f$ is $(-\infty, 2]$ .
1e.	Geen van bogenoemde

**Question 2 / Vraag 2**

Given  $f(x) = x^3 - 4x$  and  $g(x) = 1 + \cos x$ . The function  $h(x) = \frac{f(x)}{g(x)}$  is  
Gegee  $f(x) = x^3 - 4x$  en  $g(x) = 1 + \cos x$ . Die funksie  $h(x) = \frac{f(x)}{g(x)}$  is

2a.	Even / Ewe
2b.	Odd / Onewe
2c.	Neither even nor odd / Nie ewe of onewe nie
2d.	Both even and odd / Beide ewe en onewe
2e.	None of the above / Geen van bogenoemde

**Question 3 / Vraag 3**



The function  $f(x) = e^x$  and the transformed function  $g(x)$  are shown in the sketch. The function  $g(x)$  is given by  
*Die funksie  $f(x) = e^x$  en die getransformeerde funksie  $g(x)$  word beide in die skets getoon. Die funksie  $g(x)$  word gegee deur*

- |     |  |
|-----|--|
| 3a. | $g(x) = 10 - e^x$                              |
| 3b. | $g(x) = e^{-x} + 10$                           |
| 3c. | $g(x) = -e^x + 10$                             |
| 3d. | $g(x) = 10 - e^{-x}$                           |
| 3e. | None of the above / <i>Geen van bogenoemde</i> |

**Question 4 / Vraag 4**

What is the domain of  $f(x) = \ln(3 - \sqrt{x-1})$ ? / *Wat is die definisiever sameling van  $f(x) = \ln(3 - \sqrt{x-1})$ ?*

- |                 |                |                    |                     |   |
|-----------------|----------------|--------------------|---------------------|---|
| 4a. $0 < x < 4$ | 4b. $x \geq 1$ | 4c. $0 < x \leq 1$ | 4d. $1 \leq x < 10$ | 4e. None of these / <i>Geen van hierdie</i> |
|-----------------|----------------|--------------------|---------------------|---|

**Question 5 / Vraag 5**

$$\cos(\arcsin(-\frac{1}{\sqrt{2}})) = \dots \quad \cos(\operatorname{bgsin}(-\frac{1}{\sqrt{2}})) = \dots$$

- |                      |                      |                          |                           |   |
|----------------------|----------------------|--------------------------|---------------------------|---|
| 5a. $\frac{5\pi}{4}$ | 5b. $-\frac{\pi}{4}$ | 5c. $\frac{1}{\sqrt{2}}$ | 5d. $-\frac{1}{\sqrt{2}}$ | 5e. None of these / <i>Geen van hierdie</i> |
|----------------------|----------------------|--------------------------|---------------------------|---|

**Question 6 / Vraag 6**

A function  $f$  has a domain  $[-1, 1]$  and range  $[0, 2]$ . The **inverse**  $g^{-1}$  of the function  $g(x) = f(x - 1) + 1$  has 'n Funksie het as definisieversameling  $[-1, 1]$  en waardeversameling  $[0, 2]$ . Die **inverse**  $g^{-1}$  van die funksie  $g(x) = f(x - 1) + 1$  het

6a.	Domain / Definisieversameling: $[0, 2]$ Range / Waardeversameling: $[1, 3]$
6b.	Domain / Definisieversameling: $[1, 3]$ Range / Waardeversameling: $[0, 2]$
6c.	Domain / Definisieversameling: $[1, 3]$ Range / Waardeversameling: $[-2, 0]$
6d.	Domain / Definisieversameling: $[-2, 0]$ Range / Waardeversameling: $[0, 3]$
6e.	None of these / Geen van hierdie

**Question 7 / Vraag 7**

The function / Die funksie

$$f(x) = \frac{1 + e^{-\frac{1}{x}}}{1 + e^{-x}}$$

9a.	has no horizontal asymptotes / het geen horizontale asimptote nie
9b.	has one horizontal asymptote $y = 0$ / het een horizontale asimptoot $y = 0$
9c.	has one horizontal asymptote $y = 1$ / het een horizontale asimptoot $y = 1$
9d.	has one horizontal asymptote $y = 2$ / het een horizontale asimptoot $y = 2$
9e.	has two horizontal asymptotes / het twee horizontale asimptote

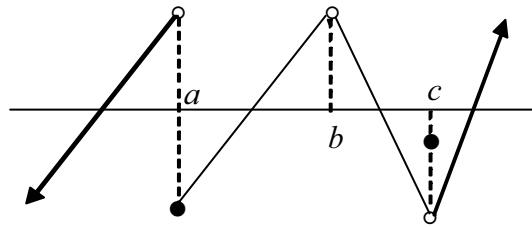
**Question 8 / Vraag 8**

$$\lim_{x \rightarrow 1^-} \frac{x - 1}{|x - 1|} = \dots$$

8a. -1	8b. 0	8c. $-\infty$	8d. 1	8e. Does not exist / Bestaan nie
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**Question 9 / Vraag 9**

The graph of  $f$  is given / Die grafiek van  $f$  word gegee



Which of the following is the statement that is **not true**? / Watter van die volgende is die bewering wat **nie waar is nie**?

7a.	$\lim_{x \rightarrow b} f(x)$ exists / bestaan
7b.	$f$ is right continuous in $a$ / $f$ is regskontinu in $a$
7c.	$\lim_{x \rightarrow a} f(x)$ does not exist / bestaan nie
7d.	$f(a)$ is undefined / is ongedefinieerd
7e.	$\lim_{x \rightarrow c} f(x) \neq f(c)$

**Question 10 / Vraag 10**

$$f(x) = \begin{cases} \frac{\sin x}{x} & \text{if } x \neq 0 \\ a & \text{if } x = 0 \end{cases}$$

Which of the following is the **true** statement? / Watter van die volgende is die bewering wat **waar** is?

10a.	The function could have a jump discontinuity depending on the value of $a$
10b.	$f(0)$ is undefined
10c.	The function has a removable discontinuity if $a \neq 1$
10d.	The function is continuous for all values of $a$
10e	All the statements are true

10a.	Die funksie mag 'n sprong-diskontinuïteit hê, afhangend van die waarde van $a$ .
10b.	$f(0)$ is ongedefinieerd
10c.	Die funksie het 'n verwyderbare diskontinuïteit vir $a \neq 1$
10d.	Die funksie is kontinu vir alle waardes van $a$
10e	Al die bewerings is waar.

**Section B / Afdeling B****Time: 45 min Marks: 20 / Tyd: 45 min Punte: 20****Question 11 / Vraag 11**

11.1 Use the graph of  $y = \ln x$  to sketch the graph of  $y = -\ln(x - 3)$ . Show all the transformations that you use.  
*Gebruik die grafiek van  $y = \ln x$  om die grafiek van  $y = -\ln(x - 3)$  te skets. Toon al die transformasies wat u gebruik.*

[3]

11.2 Solve: / Los op:  $-\ln(x - 3) \geq 1$ .

[2]

**Question 12 / Vraag 12**

Use the graph of  $f(x) = \sin x$  to solve  $\sin x \geq -\frac{1}{2}$ ,  $x \in [-\pi, \pi]$ .

Gebruik die grafiek van  $f(x) = \sin x$  om  $\sin x \geq -\frac{1}{2}$ ,  $x \in [-\pi, \pi]$  op te los.

[4]

**Question 13 / Vraag 13**

13.1 Determine / Bepaal

$$\lim_{x \rightarrow 1} \frac{\sin(x-1)}{2x^2 - x - 1}$$

[3]

13.2 Determine / Bepaal

$$\lim_{x \rightarrow \infty} \frac{2x^2 + 3\sqrt{x}}{x^5 - 8x^3 + 10}$$

[2]

**Question 14 / Vraag 14**

Let / Laat

$$f(x) = \begin{cases} \frac{\sqrt{x+4}-2}{x} & \text{if / as } x < 0. \\ 2x + a & \text{if / as } x \geq 0. \end{cases}$$

Determine  $a$  such that  $f$  is continuous in  $x = 0$ .

Bepaal  $a$  sodat  $f$  kontinu is in  $x = 0$ .

[3]

**Question 15 / Vraag 15**

Determine the vertical asymptotes, if any, of / Bepaal die vertikale asymptote, indien enige van

$$f(x) = \frac{|3x - 1|}{3x^2 + 2x - 1}$$

[3]