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GROUNDWATER GLY 265 – 2009 – PRACTICAL 1		

EXERCISE 1

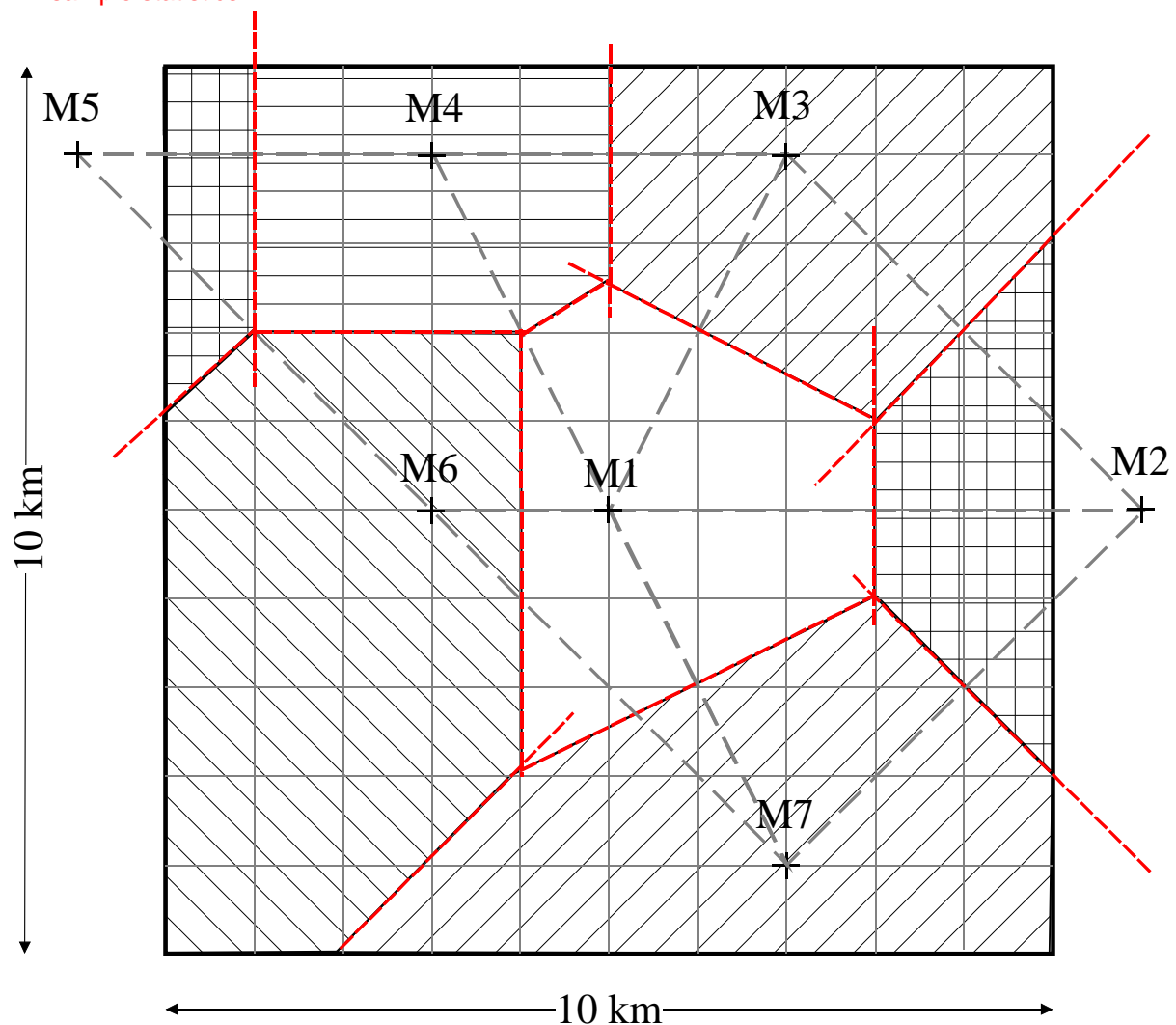
Calculate the average depth [mm] and volume [m^3] of precipitation and precipitation yield [$\text{l s}^{-1} \text{ km}^{-2}$] for the drainage basin (10 km x 10 km) using the Thiessen method.

Station	Coordinates [km]	Depth of precipitation [mm]
1	0/0	1100
2	6/0	1400
3	2/4	1300
4	-2/4	1000
5	-6/4	800
6	-2/0	900
7	2/-4	1200

SOLUTION: EXERCISE 1

Thiessen Method: Steps

1. Draw rain gage network on a map of the drainage basin
2. Connect adjacent (closest) stations by a network of lines
3. Draw a perpendicular line at the midpoint of each line connecting two stations (bisector)
4. Extensions of perpendicular bisectors build polygons around each station
5. **Weigh** each datum with the **surface area** of the polygon containing the datum and calculate global sample statistics



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$$\bar{P} = \frac{\sum P_i A_i}{\sum A_i} = \frac{P_1 A_1 + P_2 A_2 + P_3 A_3 + P_4 A_4}{A_1 + A_2 + A_3 + A_4}$$

Station	P_{st} [mm]	Area A_i [km ²]	Weighting factor $W_i = A_i / A_{total}$	$P_i = W_i * P_{st}$ [mm]
1	1100	15.50	0.155	170.5
2	1400	8.00	0.080	112.0
3	1300	15.75	0.158	204.8
4	1000	11.75	0.118	117.5
5	800	3.50	0.035	28.0
6	900	25.50	0.255	229.5
7	1200	20.00	0.200	240
		A_{total} [km ²]		$P_{av} = EUD$ [mm]
		100.00	1.00	1102.3

$$V_p = (1102.3 \times 10^3 \text{ m}^3 \cdot \text{km}^{-2}) (100 \text{ km}^2)$$

$$= 1.1 \times 10^8 \text{ m}^3$$

$$P_q = \frac{(1.1 \times 10^8 \text{ m}^3) (10^3 \text{ m}^3 \cdot \text{km}^{-3})}{100 \text{ km}^2} \times \frac{1}{(365 \text{ d} \times 24 \text{ h} \times 60 \times 60 \text{ s})}$$

$$= 34.95 \text{ l} \cdot \text{s}^{-1} \cdot \text{km}^{-2}$$

EXERCISE 2

Calculate the average depth [mm] and volume [m³] of precipitation and precipitation yield [l s⁻¹ km⁻²] for the drainage basin (figure attached) using the following methods:

- Arithmetic average
- Thiessen method
- Isohyetal method.

Station	Depth of precipitation [mm]
1	1100
2	1000
3	900
4	920
5	840
6	860
7	820

SOLUTION: EXERCISE 2

ARITHMETIC AVERAGE:

$$P_{ave} = \frac{(P_1 + P_2 + \dots + P_{12})}{12}$$

$$= 739.2 \text{ mm}$$

$$A = \text{estimated} = 25 \text{ km}^2$$

$$V_p = (739.2 \times 10^3 \text{ m}^3 \cdot \text{km}^{-2}) (11.29 \text{ km}^2)$$

$$= 1.04 \times 10^7 \text{ m}^3$$

$$P_q = \frac{(1.04 \times 10^7 \text{ m}^3) (10^3 \text{ m}^3 \cdot \text{km}^{-3})}{11.29 \text{ km}^2} \times \frac{1}{(365 \text{ d} \times 24 \text{ h} \times 60 \times 60 \text{ s})}$$

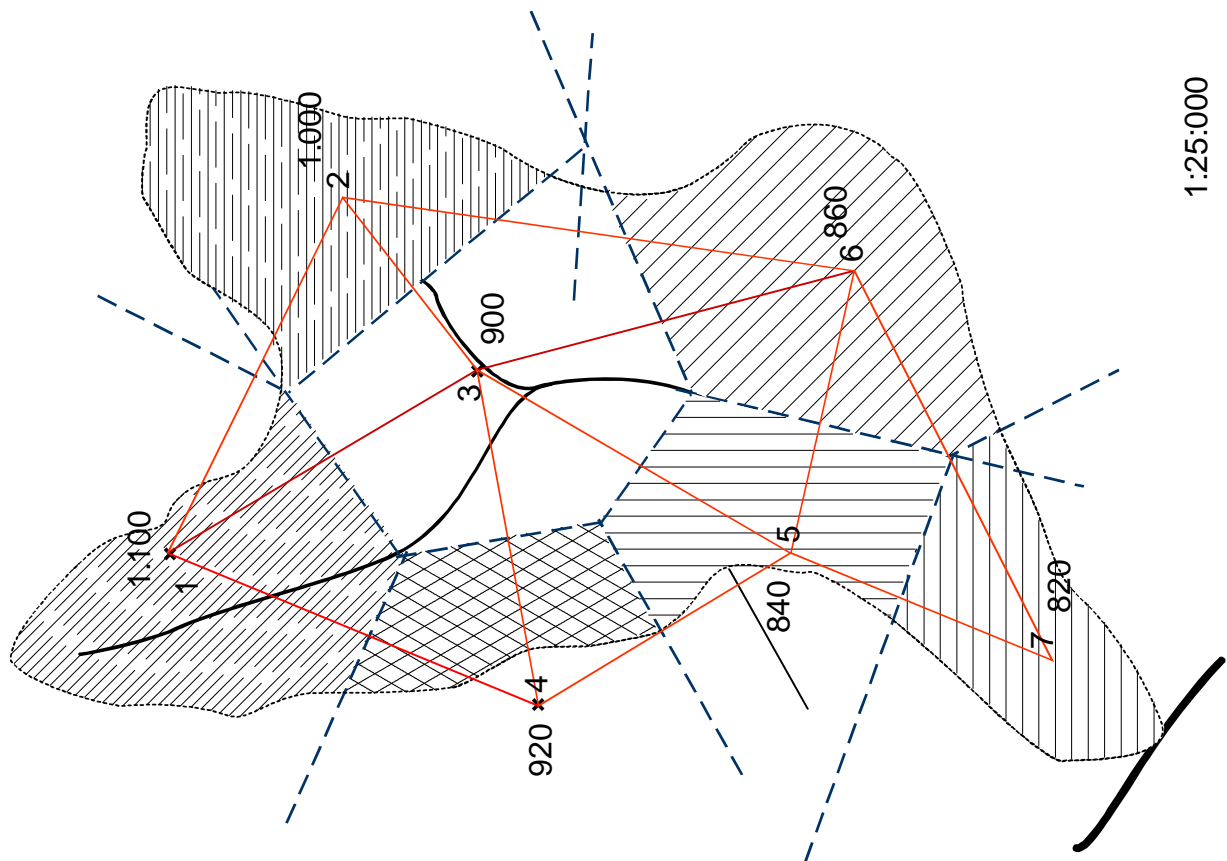
$$= 29.21 \text{ l} \cdot \text{s}^{-1} \cdot \text{km}^{-2}$$

1. Determine Effective Uniform Depth (EUD) of precipitation.

2. Calculate Volume by converting mm to m

3. Determine Precipitation Yield → Vp (km²) / Area corrected for time in seconds; 365days.

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THIESSEN:

$$V_p = (921.3 \times 10^3 \text{ m}^3 \cdot \text{km}^{-2}) (11.29 \text{ km}^2) \\ = 1.04 \times 10^7 \text{ m}^3$$

$$P_q = \frac{(1.04 \times 10^7 \text{ m}^3) (10^3 \text{ m}^3 \cdot \text{km}^{-3})}{11.29 \text{ km}^2} \times \frac{1}{(365 \text{ d} \times 24 \text{ h} \times 60 \times 60 \text{ s})} \\ = 29.21 \text{ l} \cdot \text{s}^{-1} \cdot \text{km}^{-2}$$

ISOHYETAL:

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EXERCISE 3

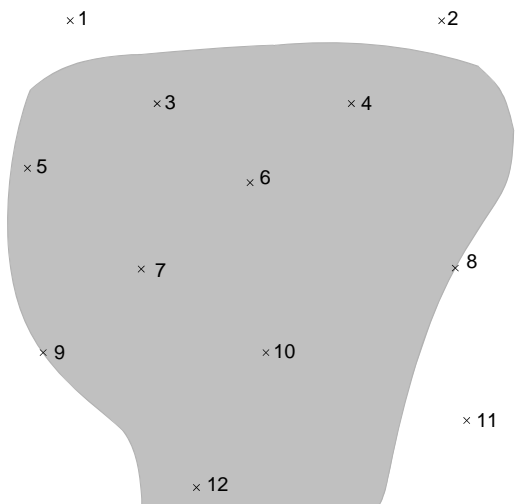
Calculate the effective uniform depth [mm] and volume [m³] of precipitation and precipitation yield [l s⁻¹ km⁻²] for the drainage basin using the following methods:

- a. Arithmetic average
- b. Thiessen method
- c. Isohyetal method
(100 m isohyets).

Station	Depth of precipitation [mm]
1	780
2	800
3	950
4	920
5	800
6	850

Station	Depth of precipitation [mm]
7	750
8	650
9	720
10	520
11	550
12	580

SOLUTION: EXERCISE 3



Arithmetic average: 739.2 mm

$V_p = 739.2 \cdot 10^3 \text{ [m}^3/\text{km}^2] \cdot 7.5 \text{ [km}^2] = 5.544 \cdot 10^6 \text{ m}^3$
 $P_q = 5.544 \cdot 10^8 \cdot 10^3 / 100 \cdot (365 \cdot 24 \cdot 60 \cdot 60) \text{ [l/s} \cdot \text{km}^2] = 23.4 \text{ l/s} \cdot \text{km}^2$

Thiessen method

	P [mm]	Area [km ²]	W _i	P _i [mm]
1	780	0.11	0.015	11.4
2	800	0.25	0.033	26.7
3	950	0.69	0.092	87.4
4	920	0.97	0.129	119.0
5	800	0.51	0.068	54.4
6	850	0.97	0.129	109.9
7	750	0.88	0.117	88.0
8	650	0.25	0.033	21.7
9	720	0.45	0.060	43.2
10	520	1.45	0.193	100.5
11	550	0.21	0.028	15.4
12	580	0.76	0.101	58.8
Σ		7.5	1.000	736.4

$N_q = 736.4 \cdot 10^3 \text{ [m}^3/\text{km}^2] \cdot 7.5 \text{ [km}^2] = 5.523 \cdot 10^6 \text{ m}^3$

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$$N_q = 5.523 \times 10^6 \times 10^3 / 7.5 \times (365 \times 24 \times 60 \times 60) \text{ [l/s*km}^2\text{]} = 23.4 \text{ l/s*km}^2$$

Isohyetal method

	P [mm]	Area [km ²]	W _i	P _i [mm]
500 – 600	550	2.00	0.267	146.7
600 – 700	650	1.25	0.167	108.3
700 – 800	750	1.65	0.220	165.0
800 – 900	850	2.00	0.267	226.7
> 900	950	0.60	0.080	76.0
Σ		7.5	1.000	722.7

$$N_Q = 722.7 \times 10^3 \text{ [m}^3\text{/km}^2\text{]} \times 7.5 \text{ [km}^2\text{]} = 5.420 \times 10^6 \text{ m}^3$$

$$N_q = 5.523 \times 10^6 \times 10^3 / 7.5 \times (365 \times 24 \times 60 \times 60) \text{ [l/s*km}^2\text{]} = 22.916 \text{ l/s*km}^2$$

EXERCISE 4

For the surface area supplied, calculate the average precipitation depth, precipitation volume and precipitation yield using the:

- Arithmetic average
- Thiessen method
- Isohyetal method.

Assuming 3% recharge of MAP and no groundwater inflows:

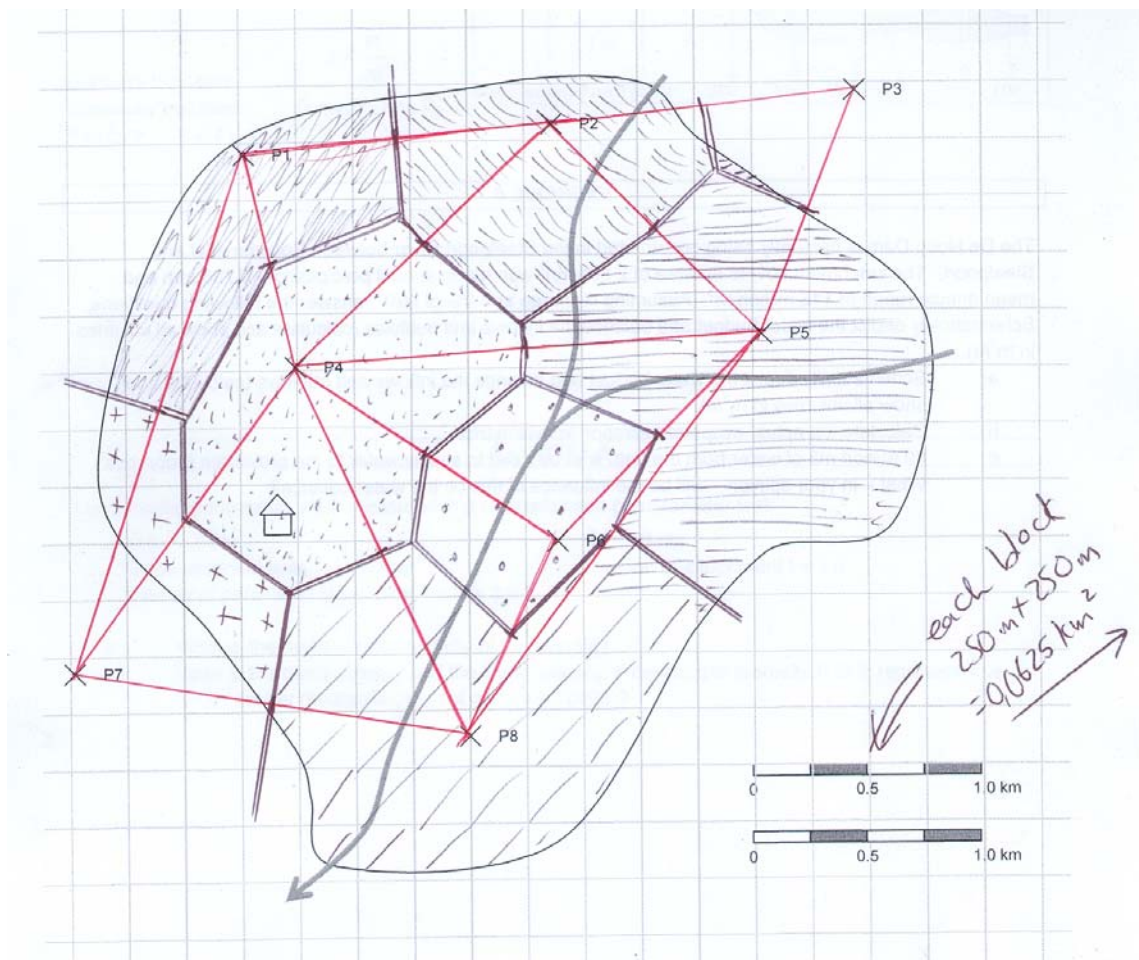
- Schematically depict the hydrological balance and the volume of water available for overland flow, interflow and baseflow.
- Address whether a farmer located at the residential dwelling can safely pump water consistently at 0.4 litres per second without affecting the streamflow.

Station	Depth of precipitation [mm]
1	980
2	1050
3	1100
4	850
5	970
6	830
7	770
8	720

SOLUTION: EXERCISE 4

- Connect three stations together to form triangles, preferably with all angles smaller than 90 degrees (if possible). → red lines on next page
- Bisect the constructed sides of the triangles to create polygons. In other words, draw a line which halves each triangle side. Aim to draw as close to perpendicular as possible and let three bisectors connect in the middle of each triangle. → double black lines on next page
- Polygons should now be completed where each station is surrounded by a polygon. Count the blocks to determine the area of each polygon as well as the total area.
- Weighting: $A_1/A = W_1$; $A_2/A = W_2$; etc. $W_1 + W_2 + W_3 + \dots + W_i = 1$.
- Calculate each station's influence on precipitation by: $P_1 = P \cdot W_1$; $P_2 = P \cdot W_2$; etc.
- Total average precipitation depth = $P_1 + P_2 + P_3 + \dots + P_i$.

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Station	Precipitation mm	blocks	Wi	Pi
1	980	13	$13/138.5 = 0.094$	$(980)(0.094) = 92\text{mm}$
2	1050	16	$16/138.5 = 0.116$	$(1050)(0.116) = 121.8\text{mm}$
3	1100	0.5	0.0036	3.96mm
4	850	26.5	0.191	162.4mm
5	970	33	0.238	230.9mm
6	830	11.5	0.083	68.9mm
7	770	7	0.051	39.3mm
8	720	31	0.224	161.3mm
		Sum = 138.5	Sum = 1	Sum = 880.6mm

Average precipitation depths = **880.6mm**

Volume of precipitation: $A = 138.5 \text{ blocks} \times 0.25\text{km} \times 0.25\text{km}$ (according to scale bar)
 $= 8.66\text{km}^2$

$$V_P = A \times P = (8.66\text{km}^2)(10^6\text{m}^2/\text{km}^2) \times (880.6\text{mm})(0.001\text{m/mm})$$

$$= 7.62 \times 10^6\text{m}^3$$

Precipitation yield:

Remember: precipitation is annual unless noted otherwise!

Therefore, convert one year to seconds!

$$P_Q = \frac{(7.62 \times 10^6\text{m}^3)(1000\text{l/m}^3)}{(8.66\text{km}^2)(365\text{d/y} \times 24\text{h/d} \times 60\text{m/h} \times 60\text{s/m})} = 0.67\text{l.s}^{-1}.\text{km}^{-2}$$