

## EXERCISE 13

The following stationary heads were measured in a confined porous aquifer after 3 days of continuous pumping at 9 l/s.

<i>Piezometer no.</i>	1	2	3	4
distance $r$ [m]	0.8	30.0	90.0	215.0
drawdown $s$ [m]	2.24	1.09	0.72	0.25

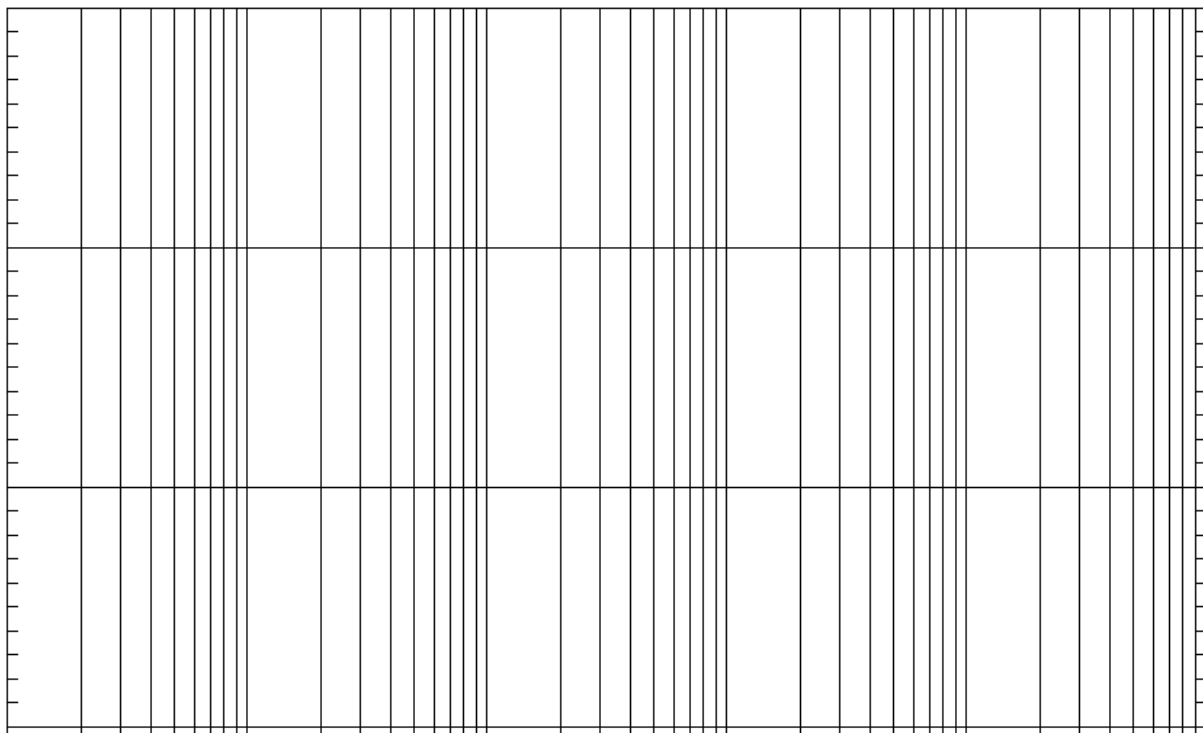
- a) Determine the transmissivity of the aquifer (graphical determination of  $\Delta h = h_2 - h_1$ ).

$$T = \frac{Q}{2\pi(\Delta h)} \ln \frac{r_2}{r_1}$$

Hint: For  $r_2/r_1 = 10 \rightarrow T = \frac{2.3Q}{2\pi(\Delta h)}$

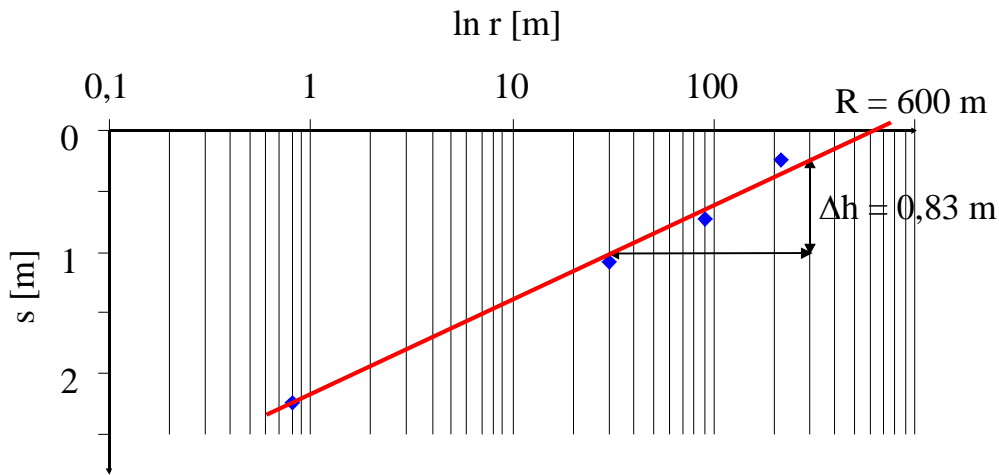
- b) Determine the extent  $R$  of the cone of depression (graphical and algebraic solution for each piezometer).

$$H - h = s = \frac{Q}{2\pi T} \ln \frac{R}{r}$$



**SOLUTION:**

- a) Plot drawdown versus  $\ln r$  and get  $\Delta h$  for one decade  
 $R_0$  for  $s = 0$  (intercept x-axis)



$\Delta h \approx 0.83 \text{ m.}$

$$H - h = s = \frac{Q}{2\pi T} \ln \frac{R}{r}$$

$$T = \frac{2.3Q}{2\pi dh} = \frac{(2.3)(0.009)}{2\pi(0.83)} = 4.0 \times 10^{-3} \text{ m}^2 \text{ s}^{-1}$$

- b) Graphical solution for  $R$ :  $R_0$  for  $s = 0$  (intercept x-axis)  
 $R = 600 \text{ m}$

Algebraic solutions:

$$H - h = s = \frac{Q}{2\pi T} \ln \frac{R}{r}$$

$$r_1 \Rightarrow R = r \cdot \exp \frac{2\pi Ts}{Q} = 0.8 \exp \frac{2\pi(4.0 \times 10^{-3})(2.24)}{0.009} = 416 \text{ m}$$

$$r_2 \Rightarrow R = r \cdot \exp \frac{2\pi Ts}{Q} = 30 \exp \frac{2\pi(4.0 \times 10^{-3})(1.09)}{0.009} = 630 \text{ m}$$

$$r_3 \Rightarrow R = r \cdot \exp \frac{2\pi Ts}{Q} = 90 \exp \frac{2\pi(4.0 \times 10^{-3})(0.72)}{0.009} = 672 \text{ m}$$

$$r_4 \Rightarrow R = r \cdot \exp \frac{2\pi Ts}{Q} = 215 \exp \frac{2\pi(4.0 \times 10^{-3})(0.72)}{0.009} = 432 \text{ m}$$

Arithmetic mean:  $R = 537.5 \text{ m.}$

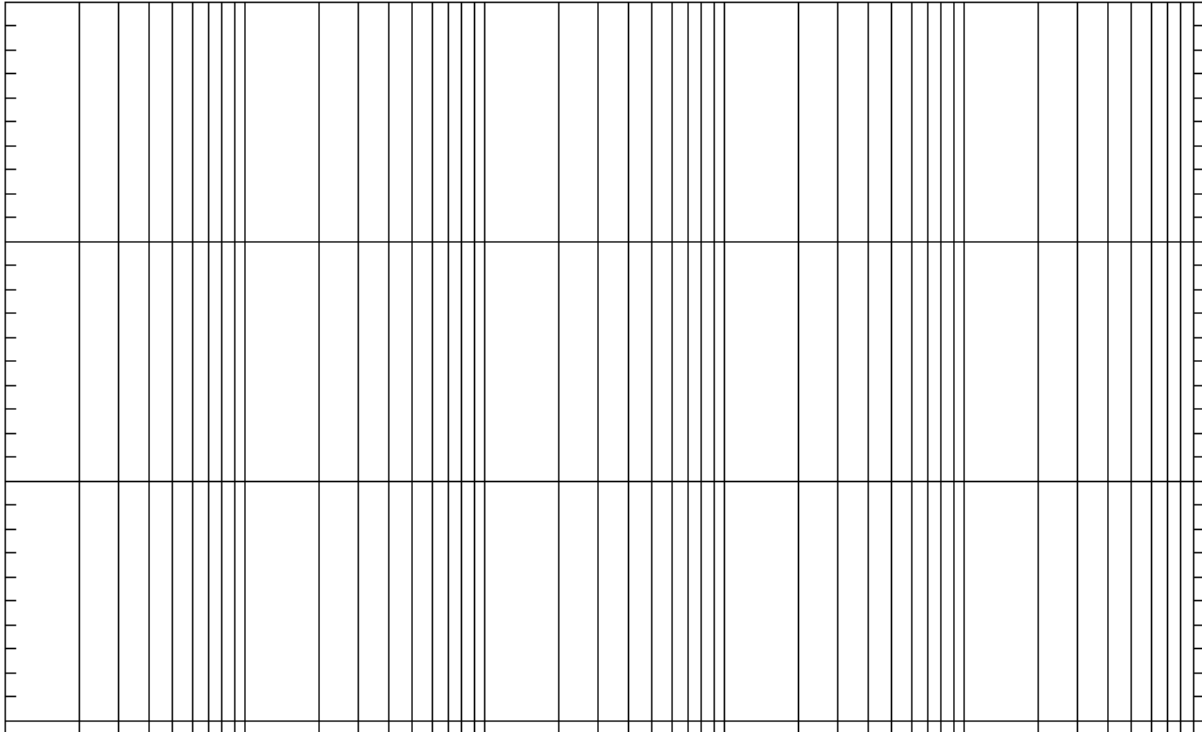
**EXERCISE 14**

The following drawdowns were measured in different piezometers during a pumping test in a confined porous aquifer ( $Q=26.7 \text{ l/s}$ ).

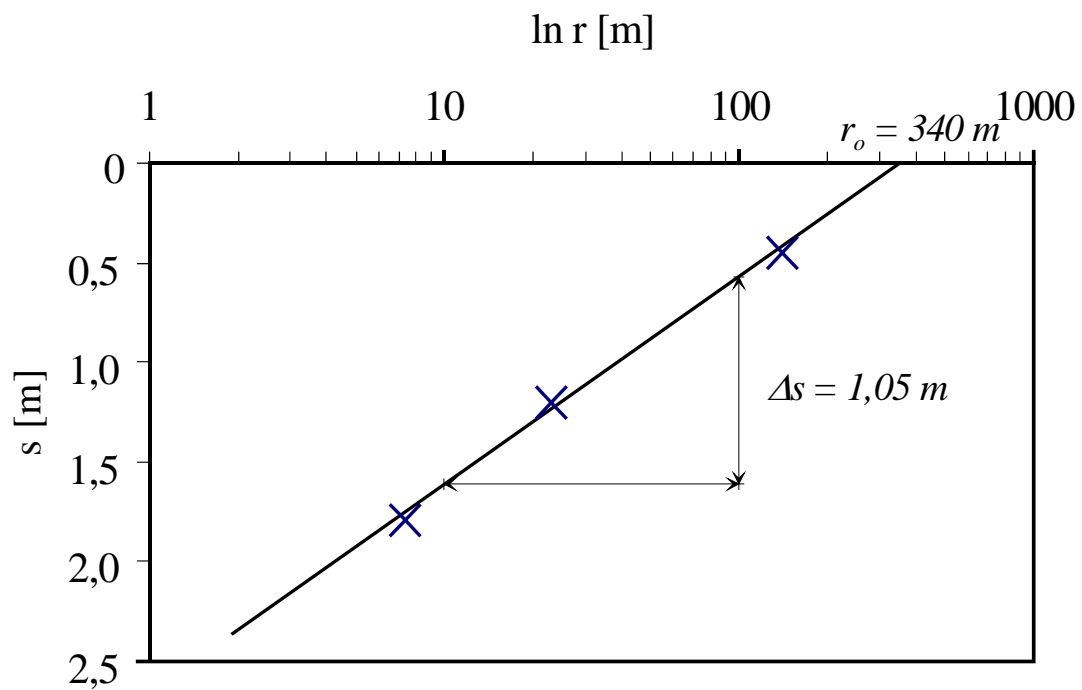
Piezometer 11 b $r = 7.40 \text{ m}$		Piezometer 3 b $r = 23.00 \text{ m}$		Piezometer 6 b $r = 139.60 \text{ m}$	
t [s]	s[m]	t[s]	s[m]	t [s]	s [m]
17	0.30	18	0.10	240	0.14
21	0.40	22	0.15	360	0.20
27	0.50	36	0.25	600	0.25
35	0.70	54	0.35	780	0.29
53	0.93	81	0.45	1140	0.35
85	1.03	122	0.55	1500	0.40
168	1.20	226	0.70	2040	0.45
220	1.28	346	0.80	2760	0.50
281	1.35	434	0.85	3900	0.55
330	1.40	549	0.90	4800	0.59
450	1.47	689	0.95	6450	0.65
540	1.50	861	1.00	8650	0.71
720	1.56	1080	1.05	11450	0.76
1080	1.64	1420	1.11	13900	0.80
1440	1.71	1800	1.15		
2100	1.79	2160	1.20		
3000	1.86	2760	1.25		
3900	1.90	3480	1.30		
5400	1.99	4380	1.35		
8300	2.07	5280	1.39		
14600	2.18	8100	1.48		
		11600	1.55		
		14150	1.50		

Determine the transmissivity  $T$  and the storage coefficient  $S$  of the aquifer using the method of Cooper-Jacob. Graphical solution for:

- $s \rightarrow \log$  (all piezometers for  $t \geq 2100 \text{ s}$ )
- $s \rightarrow \log$  (all piezometer)
- $s \rightarrow \log/r^2$

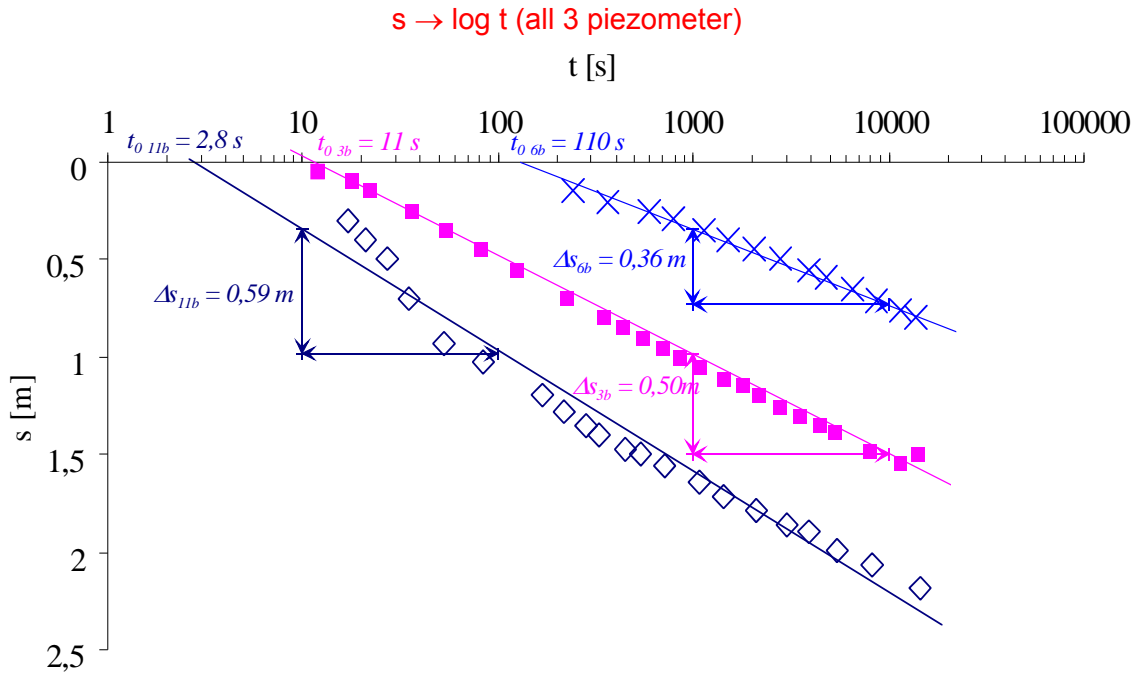
**SOLUTION:**

a)  $s \rightarrow \log r$  (all 3 piezometers for  $t \cong 2100$  s)



$$T = \frac{2.3 \cdot Q}{4\pi \Delta s} = \frac{2.3 \cdot 0.0267}{4\pi \cdot 1.05} = 0.0046 \text{ m}^2/\text{s}$$

$$S = 2.25 \cdot t \cdot T \frac{1}{r_o^2} = 2.25 \cdot 2100 \cdot 4.6 \cdot 10^{-3} \frac{1}{340^2} = 1.9 \cdot 10^{-4}$$



$$T = \frac{2.3 \cdot Q[m^3/s]}{4\pi \Delta s[m]}$$

$$T_{11b} = \frac{2.3 \cdot 0.0267}{4\pi \cdot 0.59} = 0.0082\ m^2/s;$$

$$T_{3b} = \frac{2.3 \cdot 0.0267}{4\pi \cdot 0.50} = 0.0097\ m^2/s$$

$$T_{6b} = \frac{2.3 \cdot 0.0267}{4\pi \cdot 0.36} = 0.0135\ m^2/s;$$

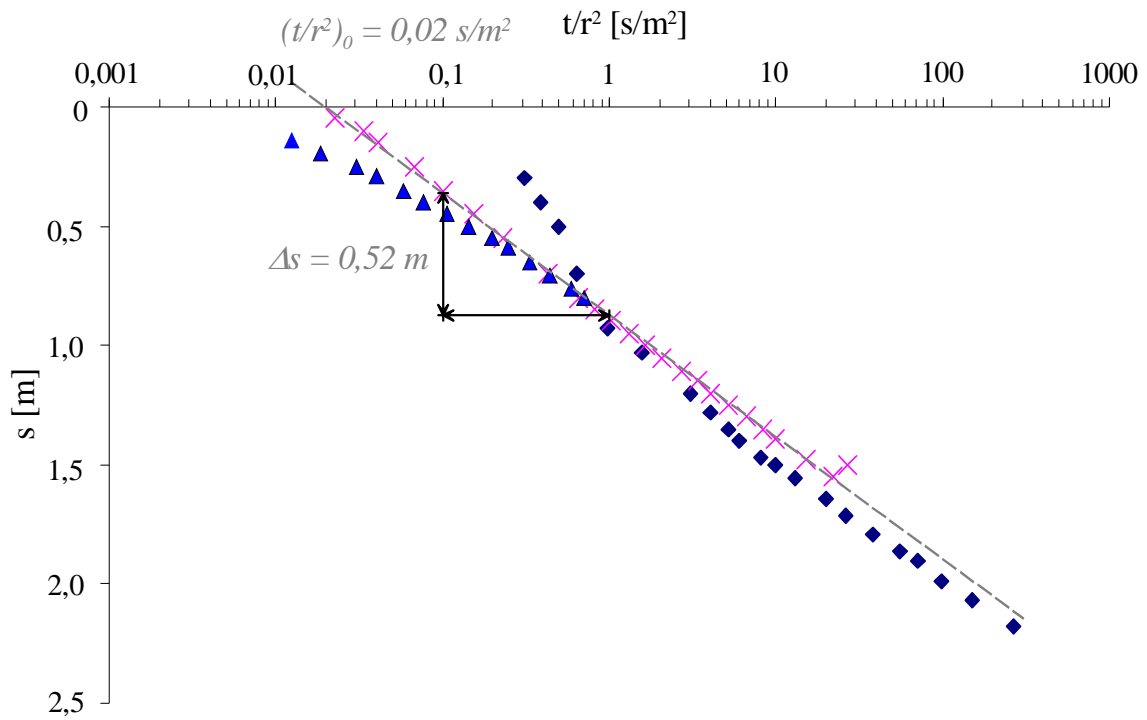
$$S = \frac{2.25 \cdot T [m^2/s]}{r^2[m^2]} \cdot t_0 [s]$$

$$S_{11b} = \frac{2.25 \cdot 0.0082}{(7.4)^2} \cdot 2.8 = 9.4 \cdot 10^{-4}$$

$$S_{3b} = \frac{2.25 \cdot 0.0097}{(23)^2} \cdot 11 = 4.5 \cdot 10^{-4}$$

$$S_{6b} = \frac{2.25 \cdot 0.0135}{(139.6)^2} \cdot 110 = 1.7 \cdot 10^{-4}$$

$s \rightarrow \log t/r^2$  (all 3 piezometer)



$$T = \frac{2.3 \cdot Q}{4\pi \Delta s} = \frac{2.3 \cdot 0.0267}{4\pi \cdot 0.52} = 0.0094 \text{ m}^2/\text{s}$$

$$S = 2.25 \cdot T \frac{t}{r_0^2} = 2.25 \cdot 0.0094 \cdot 0.02 = 4.2 \cdot 10^{-4}$$